

CS 229br Lecture 6: Causality, Fairness, Privacy

Boaz Barak



Yamini Bansal
Official TF



Javin Pombra
Official TF



Dimitris Kalimeris
Unofficial TF



Gal Kaplun
Unofficial TF

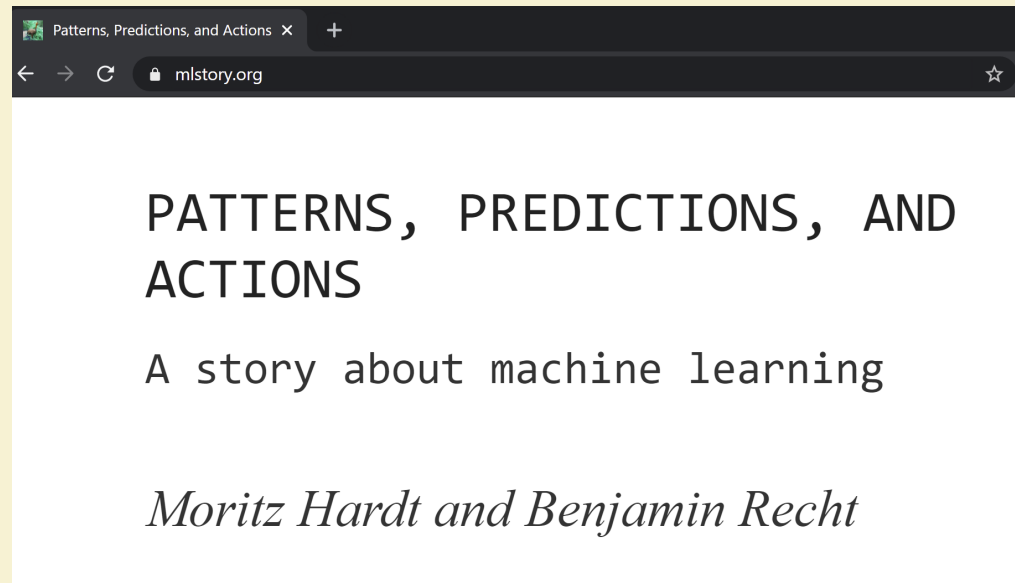
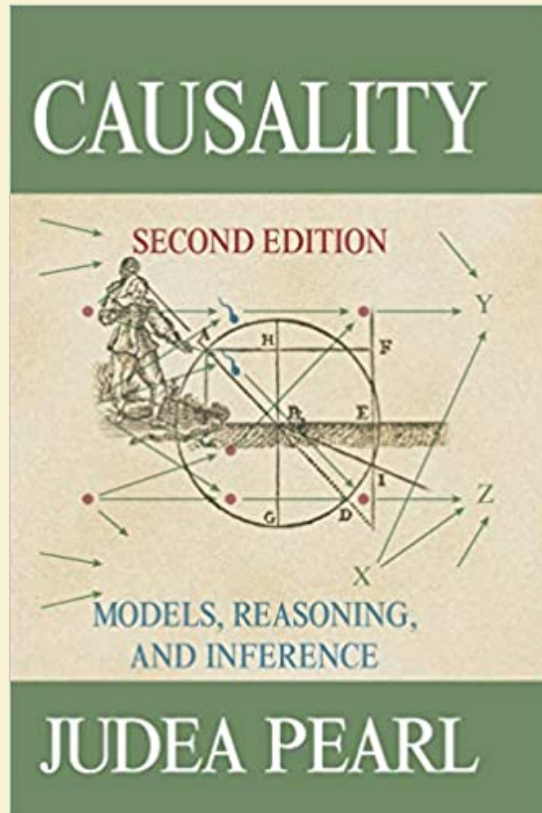


Preetum Nakkiran
Unofficial TF

Outline

- Part I: Causality
- Part II: Fairness

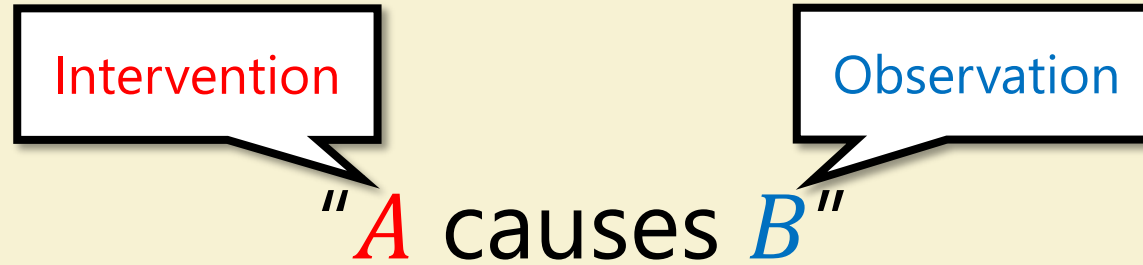
Causality



Causality

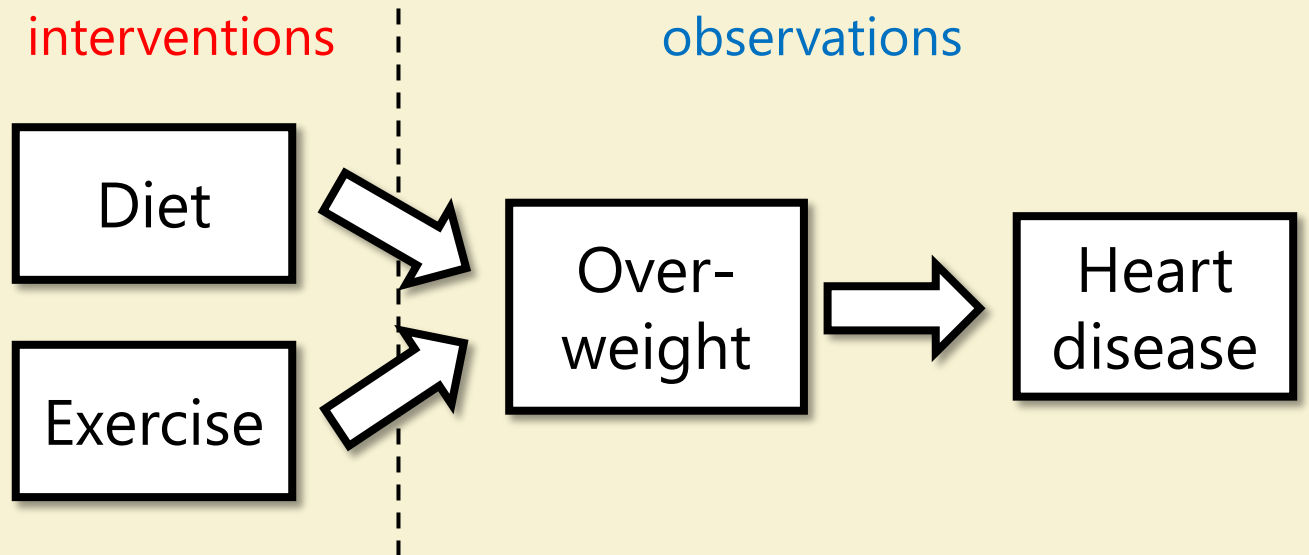
Correlation \neq Causation

But what is causation?



"Smoking causes cancer"

"Obesity causes heart disease"



Causality theory

Understand the conditions under which correlation = causation

Setup:

Observables: A, B, C, D, \dots

Interventions: "do $A \leftarrow a$ "

Correlation: $\Pr[B = b \mid A = a]$

Causation: $\Pr[B = b \mid \text{do } A \leftarrow a]$

Correlation: $\Pr[B = b \mid A = a]$

Causation: $\Pr[B = b \mid \text{do } A \leftarrow a]$

eXercise

over-
Weight

Heart
disease

Scenario 1:

$$X \leftarrow B(1/2)$$

$$W \leftarrow \begin{cases} 0, & X = 1 \\ B(1/2), & X = 0 \end{cases}$$

$$H \leftarrow \begin{cases} 0, & X = 1 \\ B(1/2), & X = 0 \end{cases}$$

X	W	H	Prob
1	0	0	1/2
0	0	0	1/8
0	0	1	1/8
0	1	0	1/8
0	1	1	1/8

Scenario 2:

$$W \leftarrow B(1/4)$$

$$X \leftarrow \begin{cases} 0, & W = 1 \\ B(1/3), & W = 0 \end{cases}$$

$$H \leftarrow \begin{cases} 0, & X = 1 \\ B(1/2), & X = 0 \end{cases}$$

	Scenario 1	Scenario 2
$\Pr[W = 1 \mid X = 0]$	1/2	1/2
$\Pr[W = 1 \mid \text{do } X \leftarrow 0]$	1/2	1/4

Correlation: $\Pr[B = b \mid A = a]$

Causation: $\Pr[B = b \mid \text{do } A \leftarrow a]$

eXercise

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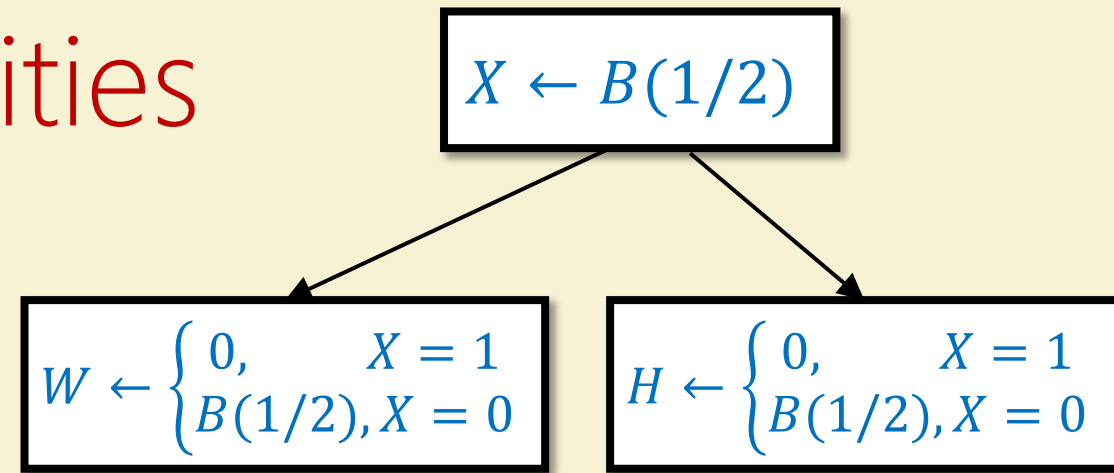
	Scenario 1	Scenario 2
$\Pr[W = 1 \mid X = 0]$	1/2	1/2
$\Pr[W = 1 \mid \text{do } X \leftarrow 0]$	1/2	1/4

Cannot distinguish Scenario 1 and 2 from observations alone!

Estimating causal probabilities

Assume: Know causal graph

Goal: Compute $\Pr[A = a | \text{do } B \leftarrow b]$



$$\Pr[H = 1 | W = 0] = 1/6$$

$$\Pr[H = 1 | \text{do } W \leftarrow 0] = 1/4$$

Controlling for X :

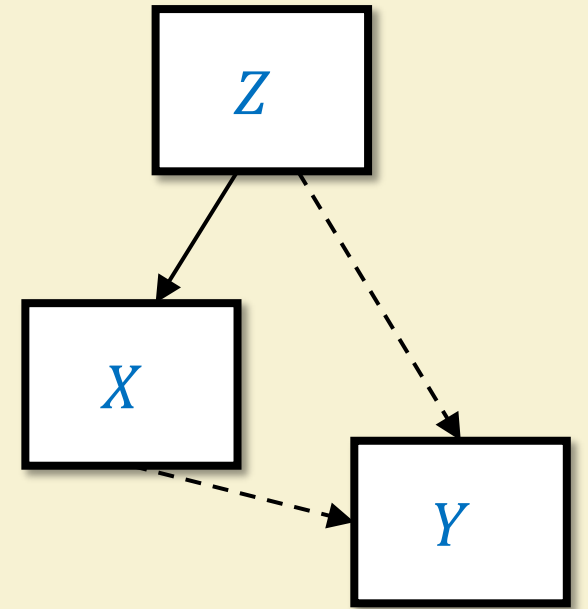
$$\begin{aligned} \Pr[H = 1 | \text{do } W \leftarrow 0] &= \Pr[H = 1 | W = 0, X = 0] \Pr[X = 0] \\ &\quad + \Pr[H = 1 | W = 0, X = 1] \Pr[X = 1] \end{aligned}$$

Apriori
unknown

Known from
observations

X	W	H	Prob
1	0	0	1/2
0	0	0	1/8
0	0	1	1/8
0	1	0	1/8
0	1	1	1/8

Adjustment formula

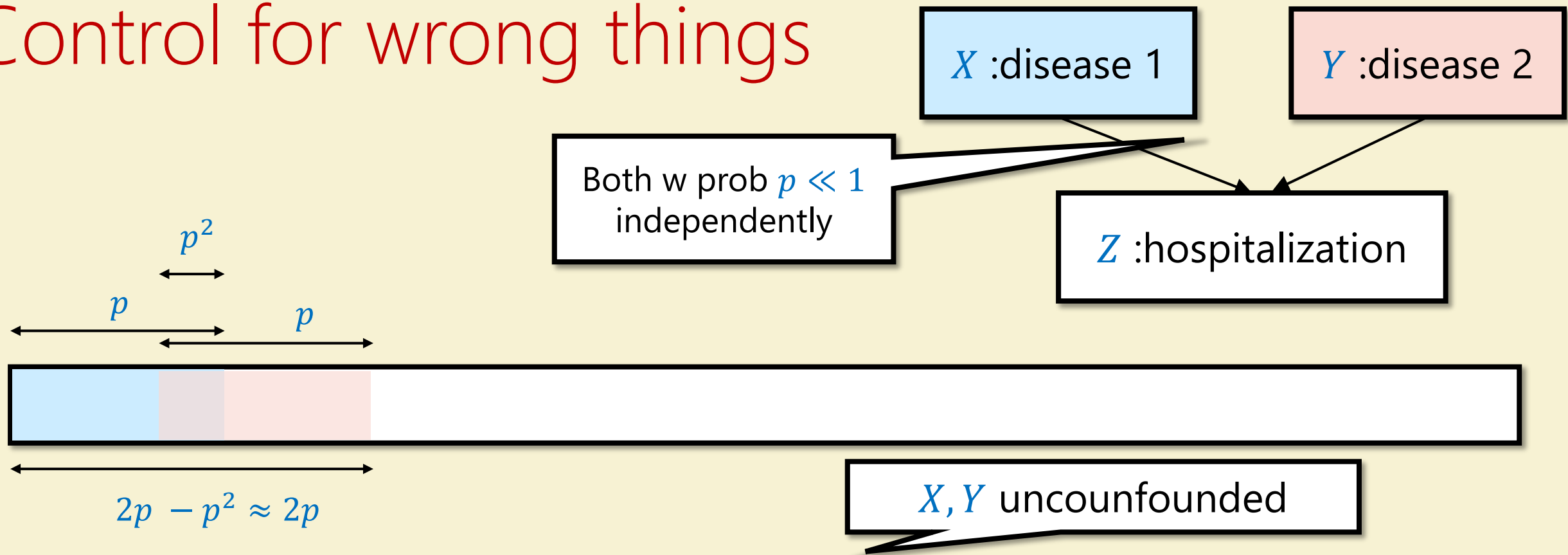


Known* from
observations

$$\Pr[Y = y \mid \text{do } X \leftarrow x] = \sum \Pr[Y = y \mid X = x, Z = z] \cdot \Pr[Z = z]$$

Apriori
unknown

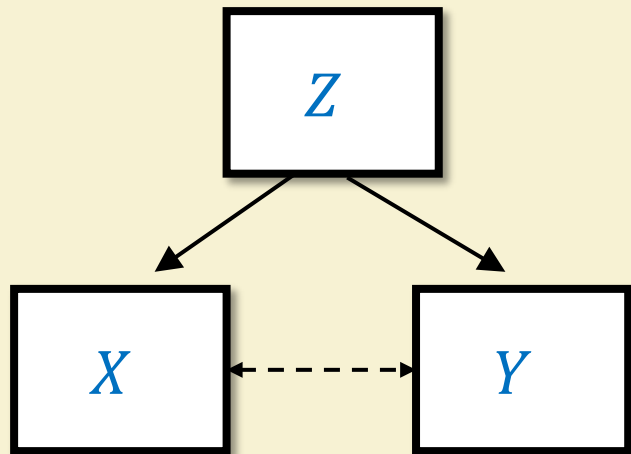
Control for wrong things



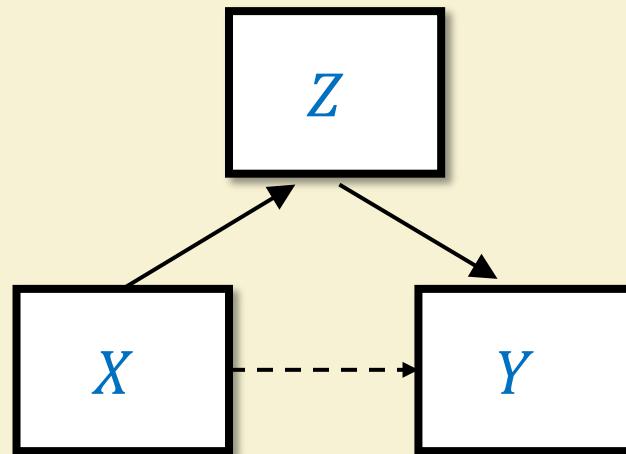
$$\Pr[X = 1|Y = 1] = \Pr[X = 1 | \text{do } Y \leftarrow 1] = p$$

Controlling for Z :

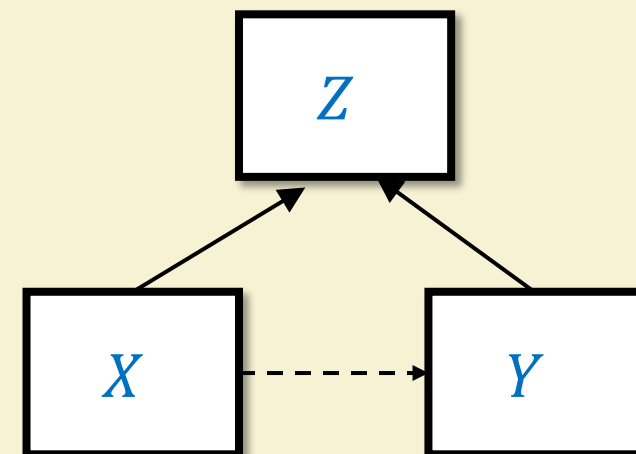
$$\begin{aligned} &\Pr[X = 1|Y = 1, Z = 1] \cdot \Pr[Z = 1] + \Pr[X = 1|Y = 1, Z = 0] \cdot \Pr[Z = 0] \approx p^2 \\ &\approx \frac{p^2}{2p} = \frac{p}{2} \qquad \approx 2p \qquad = 0 \end{aligned}$$



Fork



Mediator



Collider

$\Pr[Y = y | do X \leftarrow x]$ vs
 $\Pr[Y = y | X = x]$

\neq

$=$

$=$

$\Pr[Y = y | do X \leftarrow x]$ vs
 $\sum \Pr[Y = y | X = x, Z] \Pr[Z]$

$=$

\neq

\neq

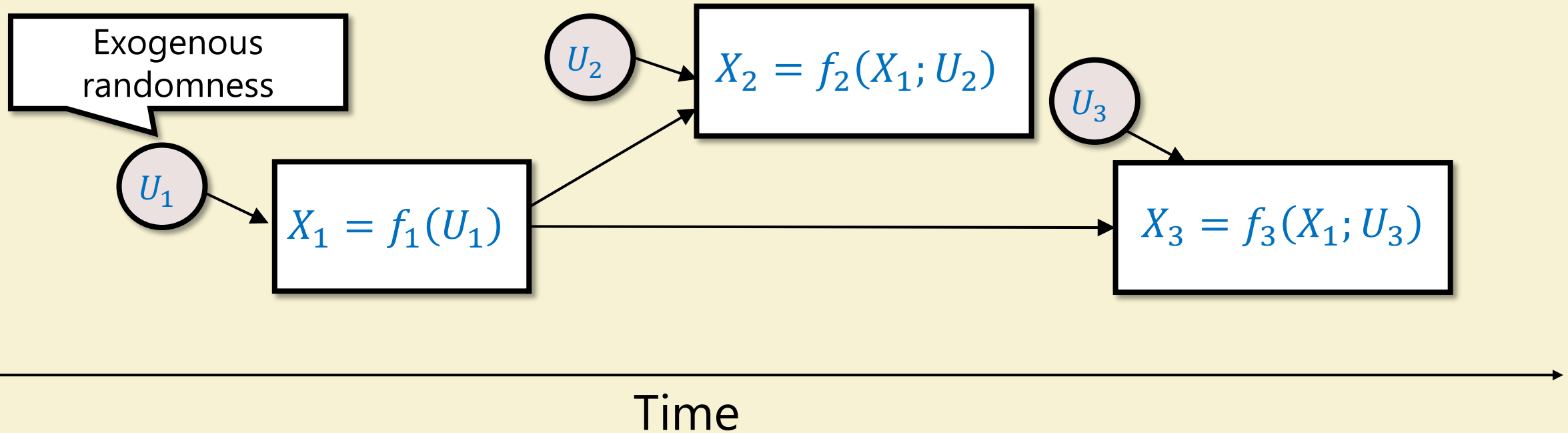
Casual Models

"Frequentist":

$\Pr[A \mid do B]$ is frequency of times that A occurs if we do B

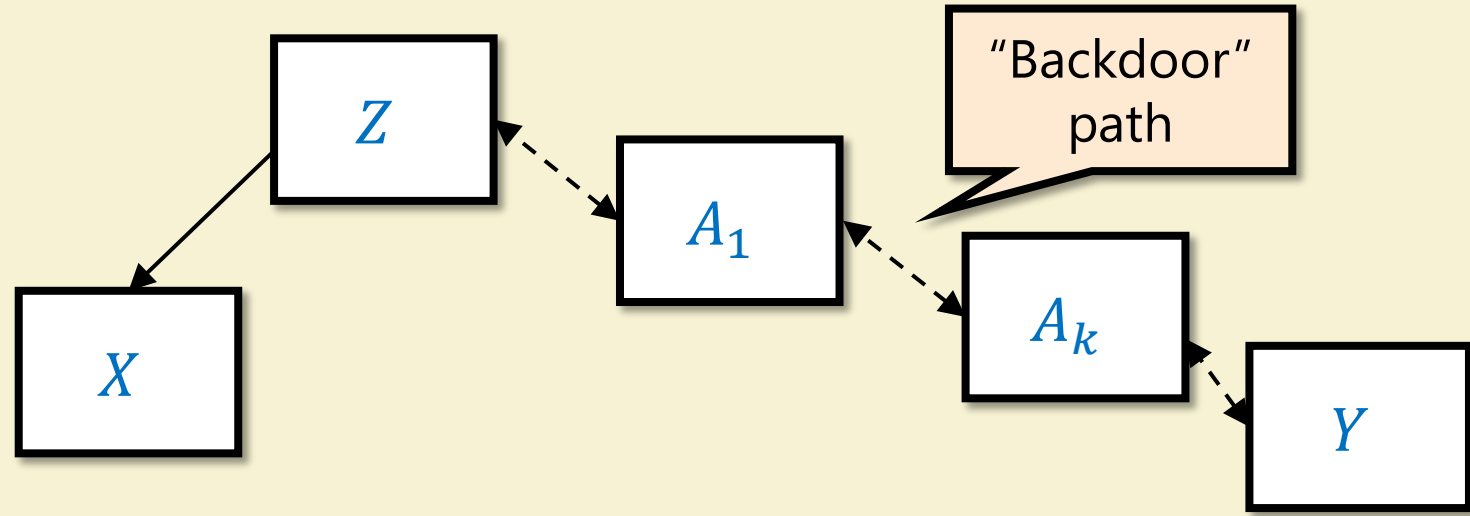
"Bayesian":

$\Pr[A \mid do B]$ is probability A would have happened in "counter-factual" world where we did B



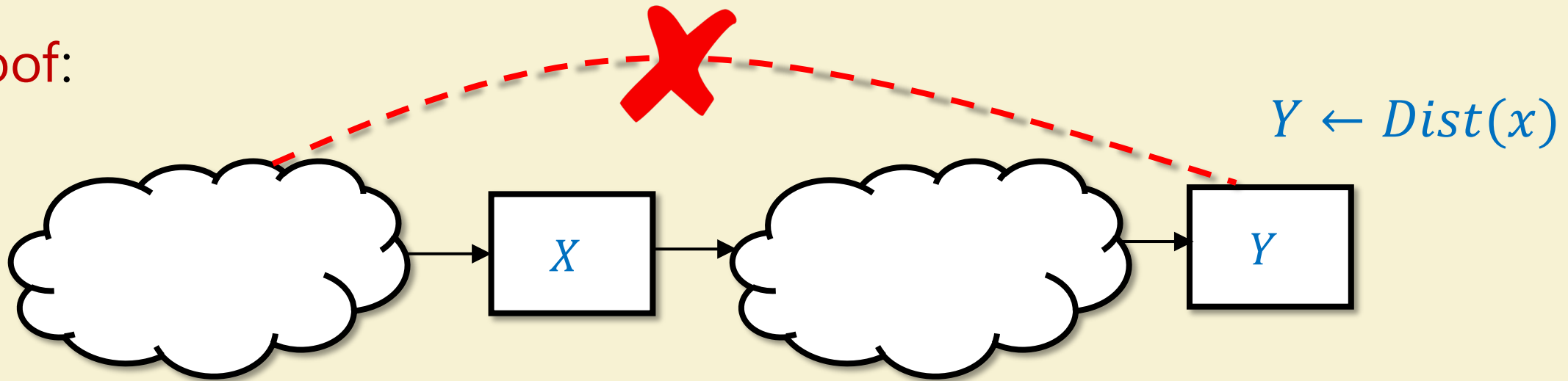
Backdoors

Def: X, Y are confounded if

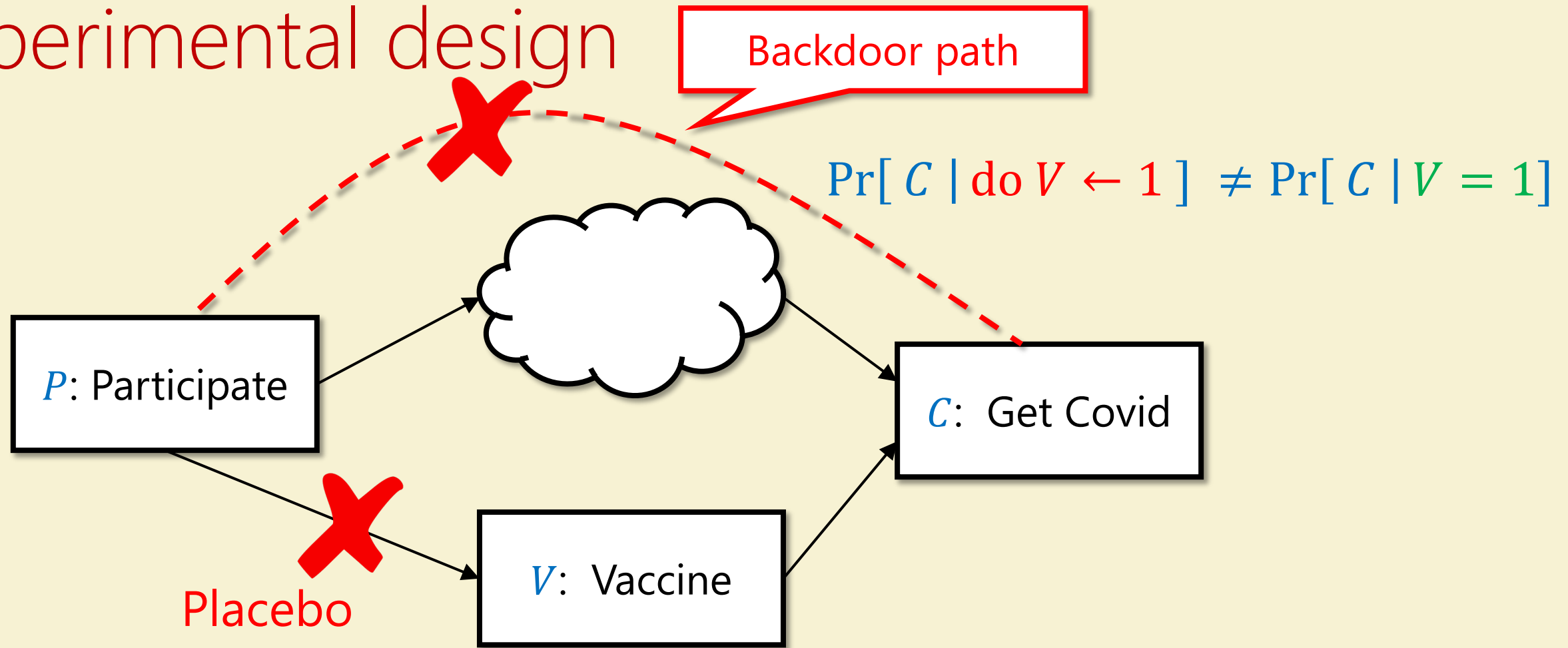


Thm: If X, Y not confounded then $\Pr[Y = y | \text{do } X \leftarrow x] = \Pr[Y = y | X = x]$

Proof:

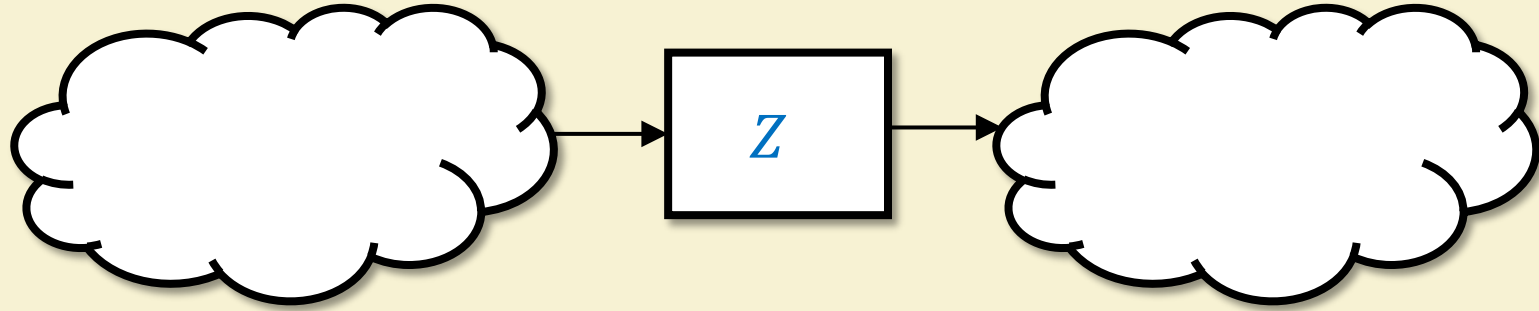


Experimental design

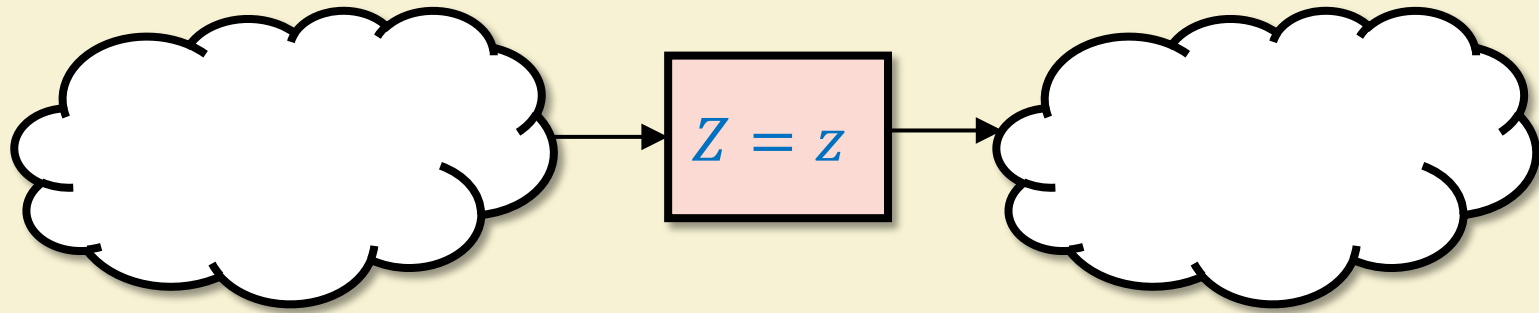


Treatment effect: $\Pr[C | \text{do } V \leftarrow 1, P]$ vs $\Pr[C | \text{do } V \leftarrow 0, P]$

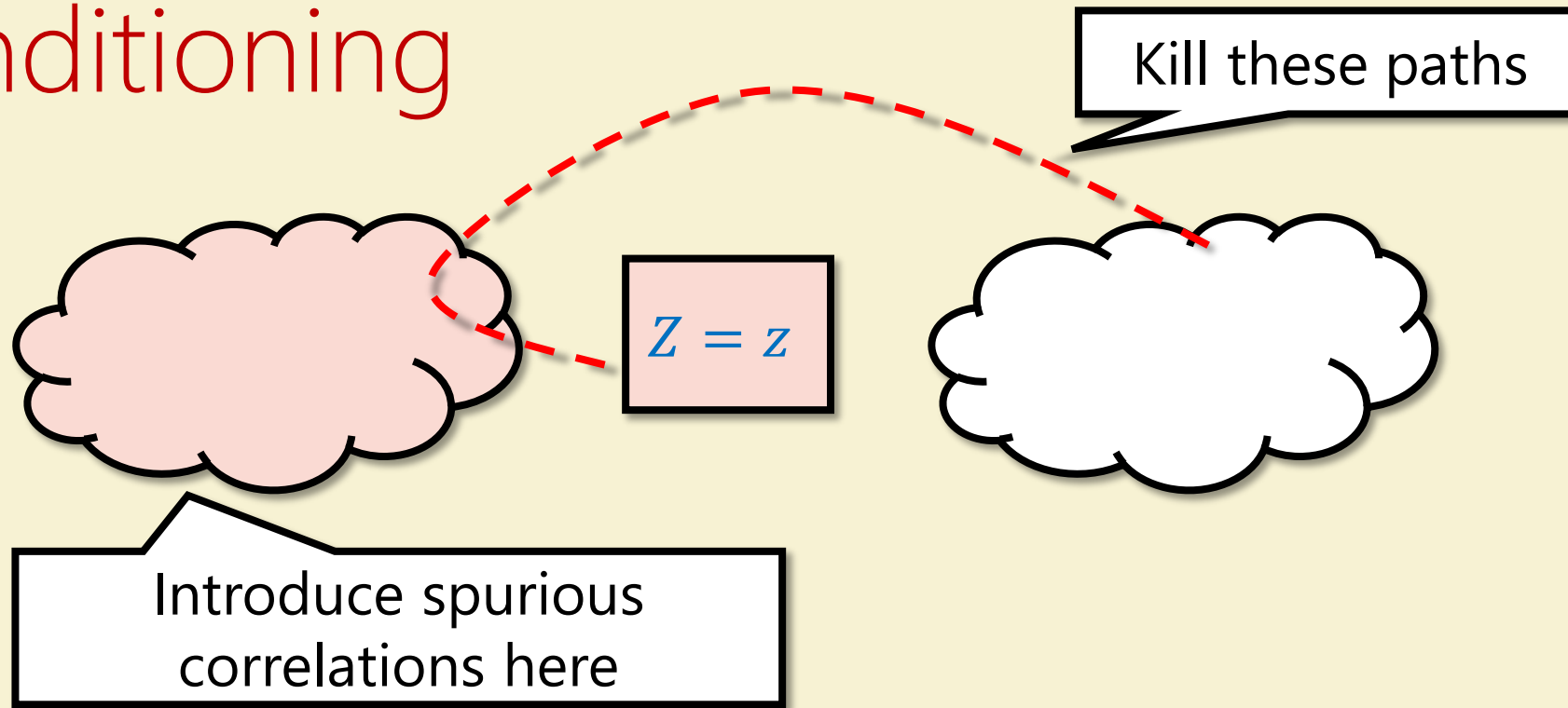
Conditioning



Conditioning

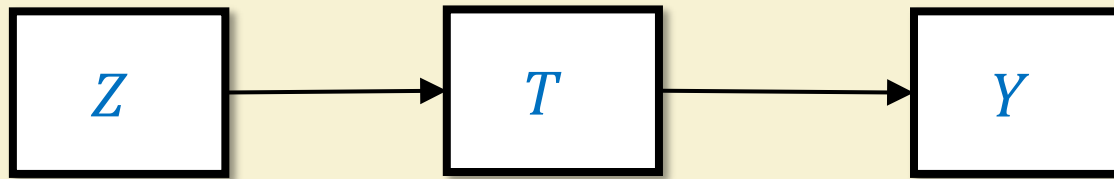


Conditioning



Average Treatment Effect

$T \in \{0,1\}$ – Treatment variable



$Y_t: Y \mid \text{do } T \leftarrow t$

Goal: Estimate $\mathbb{E}[Y_1] - \mathbb{E}[Y_0]$

aka Z "admissible"

Def: T, Y "ignorable" controlling for Z if:

$T \perp (Y_0, Y_1) \mid Z$ i.e: choice of $T = 0,1$ independent of $Y \mid \text{do } T \leftarrow t$

Average Treatment Effect

$T \in \{0,1\}$ – Treatment variable

Goal: Estimate $\mathbb{E}[Y_1] - \mathbb{E}[Y_0]$

Def: T, Y “ignorable” controlling for Z if:

$T \perp (Y_0, Y_1) \mid Z$ i.e: choice of $T = 0,1$ independent of $Y \mid \text{do } T \leftarrow t$

Claim: If T, Y ignorable controlling for Z then

$$\Pr[Y = y \mid \text{do } T \leftarrow t] = \sum \Pr[Y = y \mid T = t, Z = z] \Pr[Z = z]$$

Pf:

$$\sum \Pr[Y = y \mid T = 0, Z = z] \Pr[Z = z] = \sum \Pr[Y_0 = y \mid Z = z] \Pr[Z = z]$$

Propensity scores:

Learn model $e(z) \approx \mathbb{E}[T|Z = z]$

Let $e(z) = \mathbb{E}[T|Z = z]$

CLAIM: If Z admissible, $\mathbb{E}[Y | \text{do } T \leftarrow 1] = \mathbb{E}\left[\frac{Y \cdot T}{e(Z)}\right]$

Pf: $\Pr[Y = y | \text{do } T \leftarrow 1] = \sum_z \Pr[Y = y | T = 1, z] \Pr[z]$

For $y \neq 0$

$$= \sum_z \Pr[z] \frac{\Pr[Y=y, T=1|z]}{\Pr[T=1|z]} = \mathbb{E}_z \left[\frac{\Pr[Y=y, T=1 | z]}{e(Z)} \right] = \mathbb{E}_z \left[\frac{\Pr[YT=y|z]}{e(Z)} \right]$$

$$\mathbb{E}[Y | \text{do } T \leftarrow 1] = \sum_y \Pr[Y = y | \text{do } T \leftarrow 1] \cdot y$$

$$= \sum_y \mathbb{E}_z \left[\frac{\Pr[YT = y|z] y}{e(Z)} \right] = \mathbb{E}_z \left[\frac{Y \cdot T}{e(Z)} \right]$$



Double ML

Learn model $e(z) \approx \mathbb{E}[T|Z = z]$

Let $e(z) = \mathbb{E}[T|Z = z]$

Assume $Y = \psi(Z) + \tau \cdot T + \text{Noise}$

τ = treatment effect

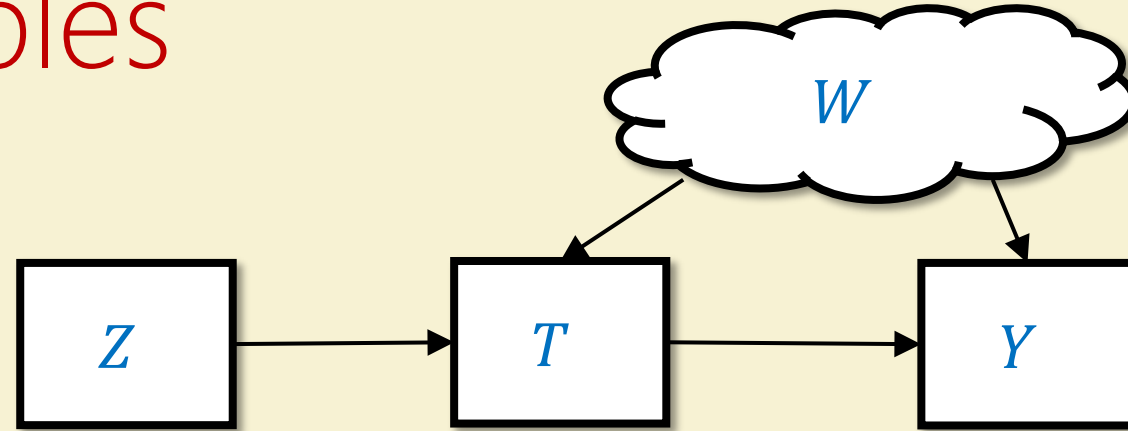
Observe (Z, T, Y) , learn model $f(z) \approx \mathbb{E}[Y|Z = z]$

$$f(z) \approx \psi(Z) + \tau \cdot e(z)$$

$$\Rightarrow Y - f(z) \approx \tau \cdot (T - e(z))$$

Can estimate from data

Instrumental variables



W is unobserved: can't control for

Assume $Y = \tau \cdot T + f(W)$ $Cov(Z, f(W)) = 0$

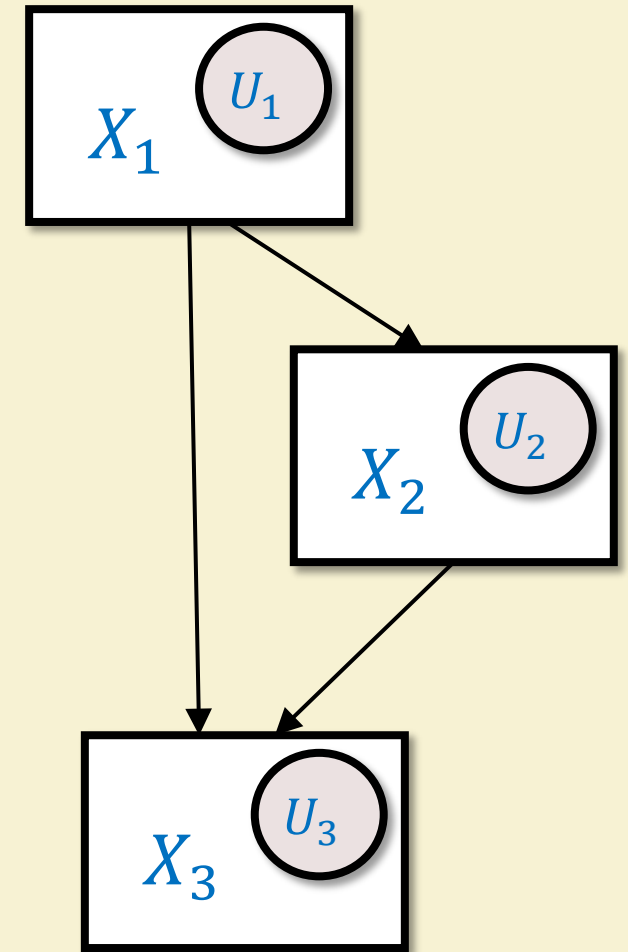
τ = treatment effect

$$\Rightarrow \tau = \frac{Cov(Z, Y)}{Cov(Z, T)}$$

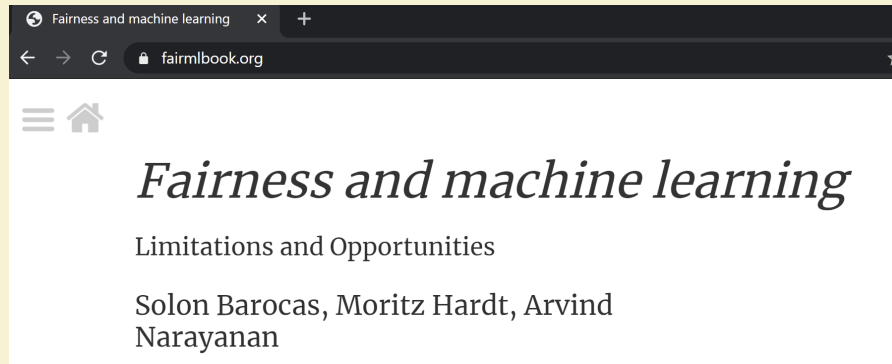
Counterfactuals

Let u realization of $U_1 \dots U_n$

$Y_{X \leftarrow x}(u)$ = output of Y if $U = u$ and $X = x$



Fairness



NIPS 2017 Tutorial on Fairness in Machine Learning

Solon Barocas, Moritz Hardt

Note: Focus on fairness in **classification**, not **representation**

On the Dangers of Stochastic Parrots: Can Language Models Be Too Big? 🦜

Emily M. Bender*
ebender@uw.edu
University of Washington
Seattle, WA, USA

Angelina McMillan-Major
aymm@uw.edu
University of Washington
Seattle, WA, USA

Timnit Gebru*
timnit@blackinai.org
Black in AI
Palo Alto, CA, USA

Shmargaret Shmitchell
shmargaret.shmitchell@gmail.com
The Aether

NEWS

Google Algorithm Detects Lung Cancer Better Than Human Doctors

Replaced by Cheaper Software

YOUR JOB?

BY STEPHANIE MLOT 05.21.2019 :: 8:

STEVEN LEVY 04.24.12 04:46 PM



By Gary M

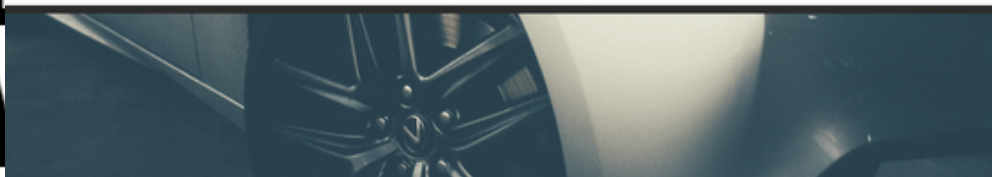
Can an Algorithm Write a Better News Story Than a Human Reporter?



Are Self-Driving Cars on the Road to

OVERTAKING TRADITIONAL VEHICLES?

Nikolas Perrault



ROBO RECRUITING

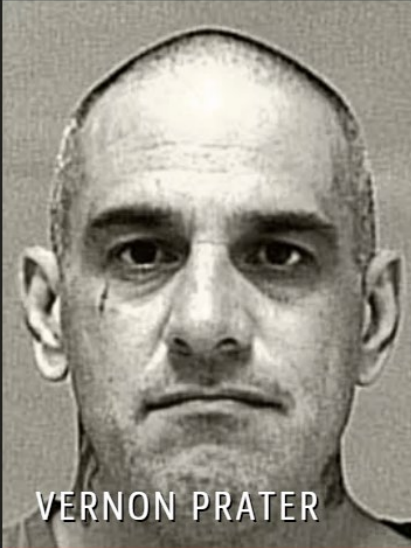
Can an Algorithm Hire Better Than a Human?



Claire Cain Miller @clairecm JUNE 25, 2015

Hiring and recruiting might seem like some of the least likely jobs to be automated. The whole process seems to need human skills that computers

Risk of Recidivism




VERNON PRATER

Prior Offenses
2 armed robberies, 1
attempted armed
robbery

Subsequent Offenses
1 grand theft

LOW RISK **3**




VERNON PRATER

Prior Offenses
2 armed robberies, 1
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Subsequent Offenses
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LOW RISK **3**

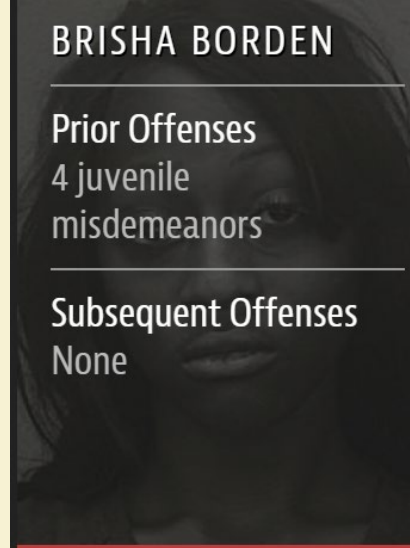


BRISHA BORDEN

Prior Offenses
4 juvenile
misdemeanors

Subsequent Offenses
None

HIGH RISK **8**



BRISHA BORDEN

Prior Offenses
4 juvenile
misdemeanors

Subsequent Offenses
None

HIGH RISK **8**

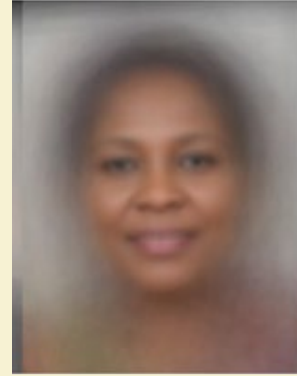
	WHITE	AFRICAN AMERICAN
Labeled Higher Risk, But Didn't Re-Offend	23.5%	44.9%
Labeled Lower Risk, Yet Did Re-Offend	47.7%	28.0%

Angwin, Larson, Mattu, Kirchner 2016

Gender detection



99.7% correct



65.3% correct

Buolamwini, Gebru, 2018

Non-ML unfairness


Are Emily and Greg More Employable Than Lakisha and Jamal? A Field Experiment on Labor Market Discrimination

Marianne Bertrand
Sendhil Mullainathan

AMERICAN ECONOMIC REVIEW
VOL. 94, NO. 4, SEPTEMBER 2004
(pp. 991-1013)

*“White names receive **50 percent more callbacks** for interviews. Callbacks are also more **responsive to resume quality** for White names than for African-American ones.”*

Meta-analysis of field experiments shows no change in racial discrimination in hiring over time

 Lincoln Quillian, Devah Pager, Ole Hexel, and Arnfinn H. Midtbøen

[+ See all authors and affiliations](#)

PNAS October 10, 2017 114 (41) 10870-10875; first published September 12, 2017;

Algorithms help?

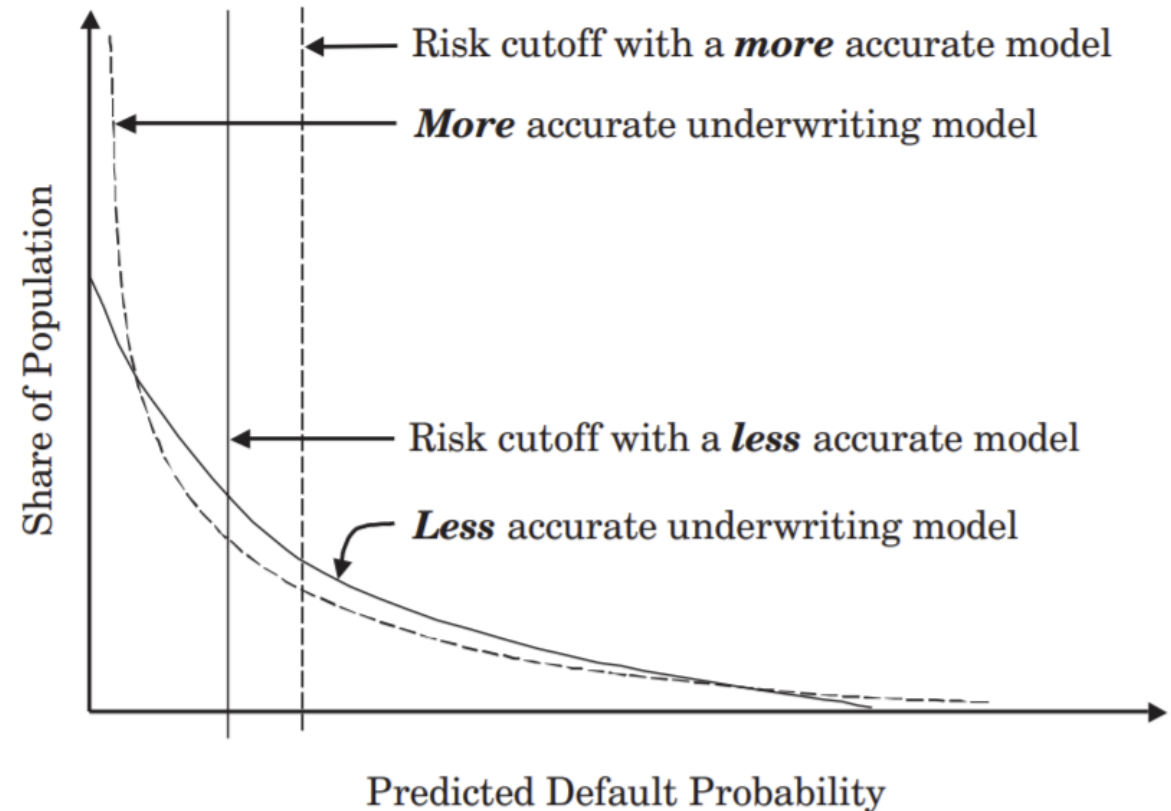
Original Articles

Automated underwriting in mortgage lending: Good news for the underserved?

Susan Wharton Gates, Vanessa Gail Perry & Peter M. Zorn

Pages 369-391 | Published online: 31 Mar 2010

Figure 6. Effect of Introducing More Accurate Underwriting Models

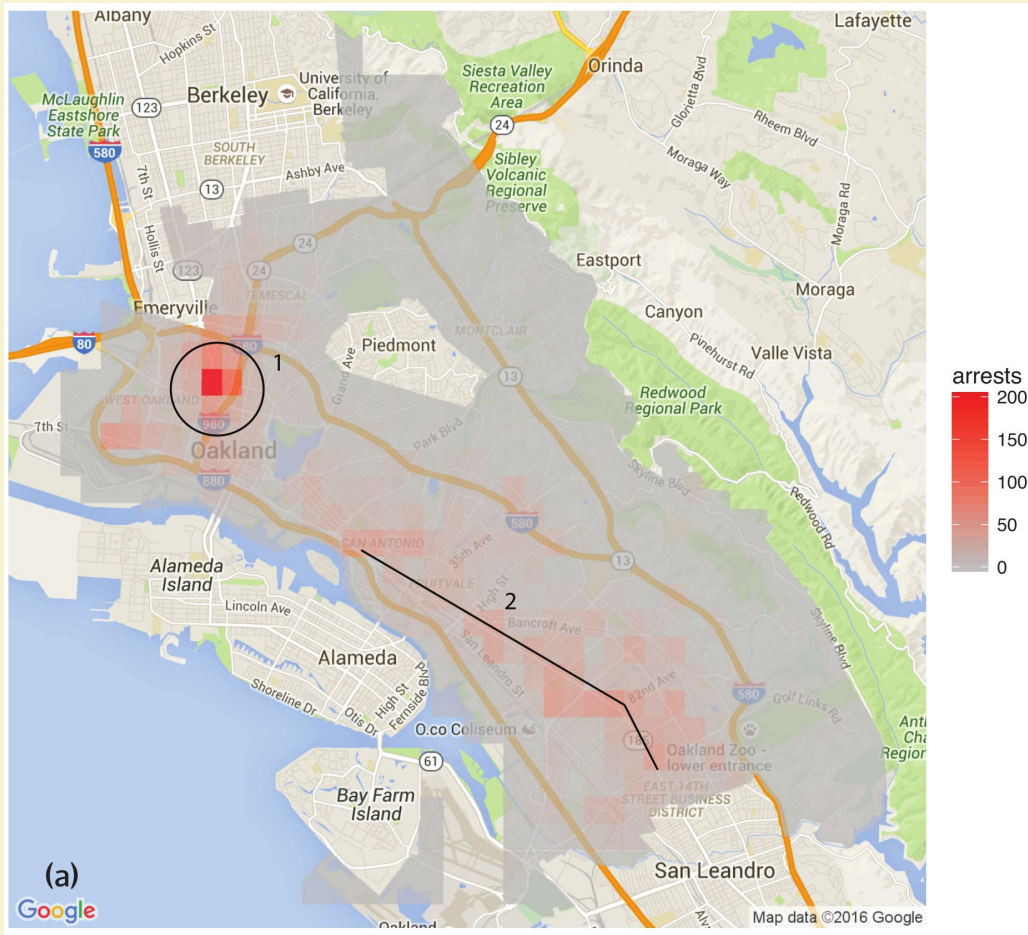


To predict and serve?

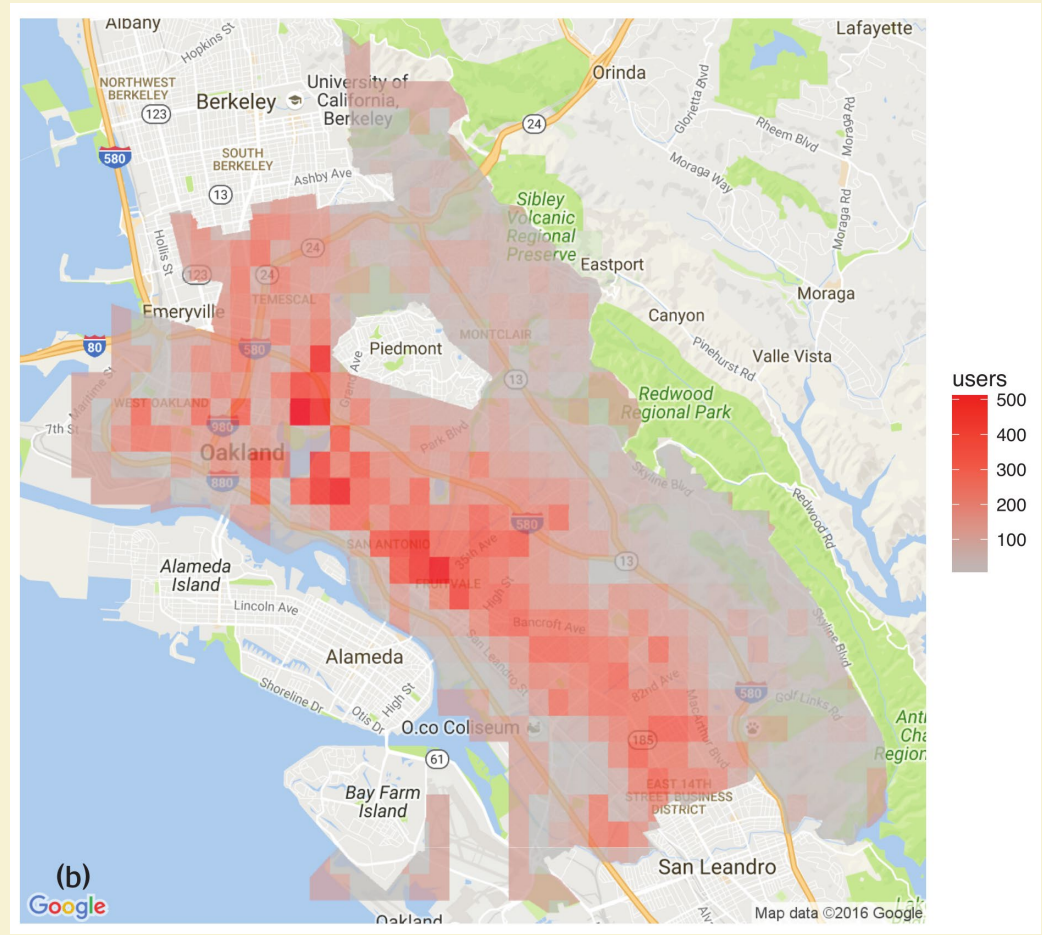
Predictive policing systems are used increasingly by law enforcement to try to prevent crime before it occurs. But what happens when these systems are trained using biased data?

Kristian Lum and **William Isaac** consider the evidence – and the social consequences



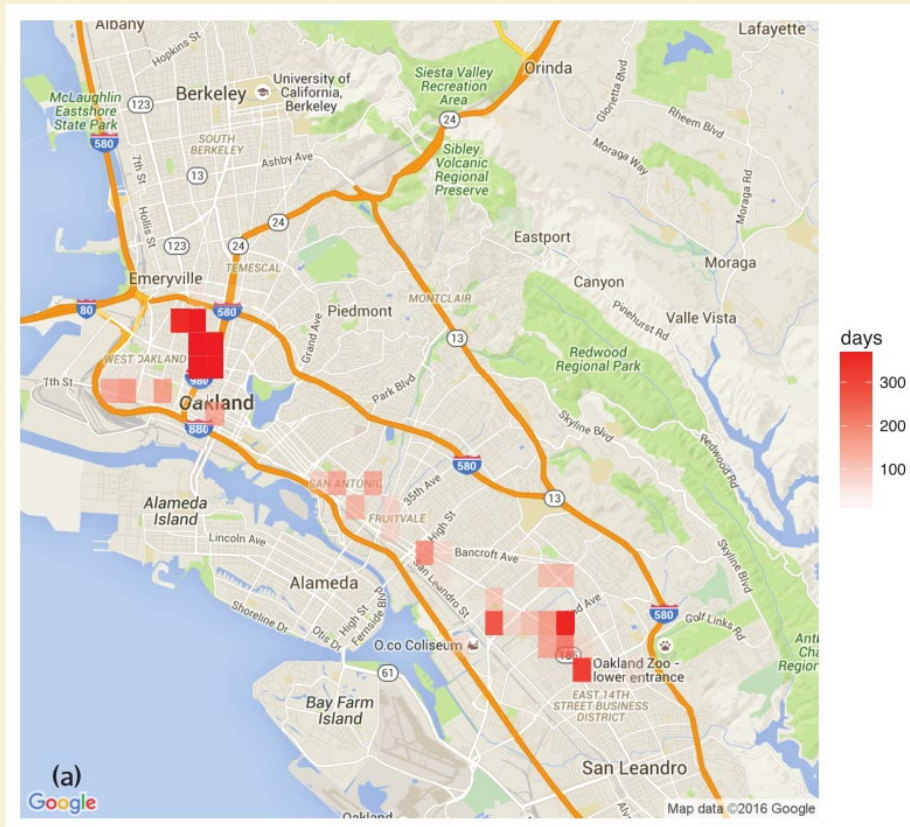


Arrests



Drug usage

Positive feedback loop



Predicted crime

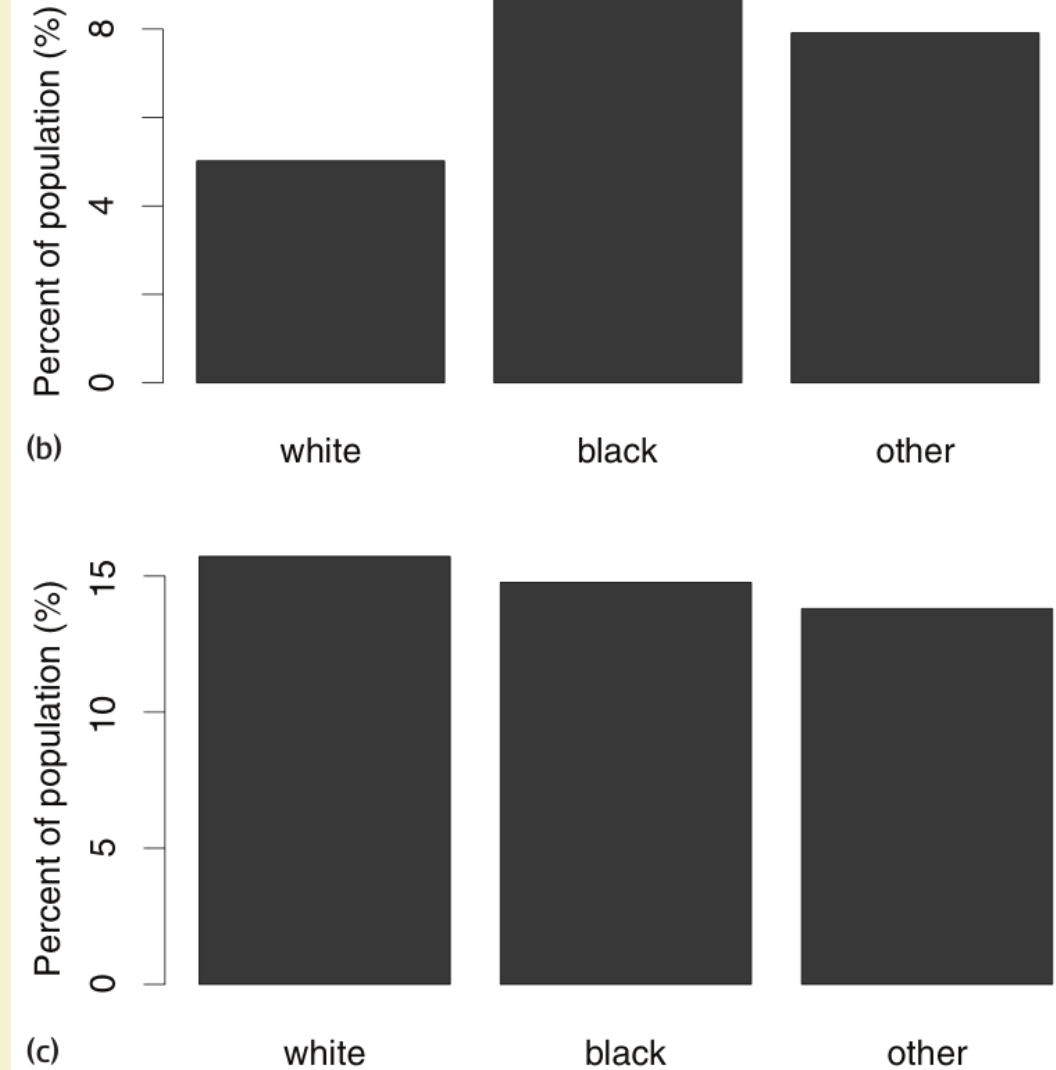


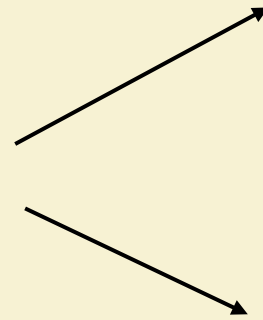
FIGURE 2 (a) Number of days with targeted policing for drug crimes in areas flagged by PredPol analysis of Oakland police data. (b) Targeted policing for drug crimes, by race. (c) Estimated drug use by race

Making it formal

Unfairness definitions

Components:

- Protected class*
- Unfairness measurement



Disparate treatment

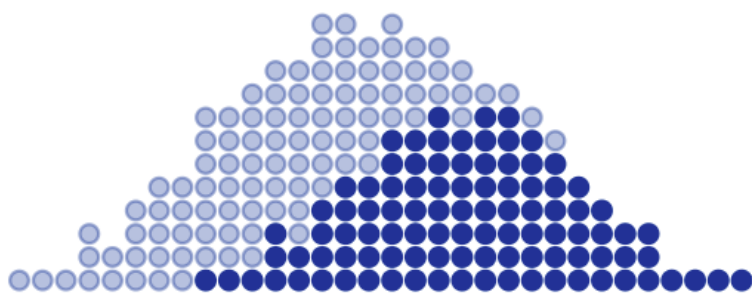
Disparate impact

Race (Civil Rights Act of 1964); **Color** (Civil Rights Act of 1964); **Sex** (Equal Pay Act of 1963; Civil Rights Act of 1964); **Religion** (Civil Rights Act of 1964); **National origin** (Civil Rights Act of 1964); **Citizenship** (Immigration Reform and Control Act); **Age** (Age Discrimination in Employment Act of 1967); **Pregnancy** (Pregnancy Discrimination Act); **Familial status** (Civil Rights Act of 1968); **Disability status** (Rehabilitation Act of 1973; Americans with Disabilities Act of 1990); **Veteran status** (Vietnam Era Veterans' Readjustment Assistance Act of 1974; Uniformed Services Employment and Reemployment Rights Act); **Genetic information** (Genetic Information Nondiscrimination Act)

Blue Population

0 10 20 30 40 50 60 70 80 90 100

loan threshold: 0

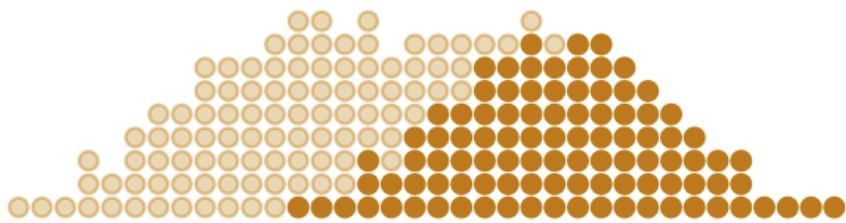


denied loan / would default light blue
denied loan / would pay back dark blue granted loan / defaults
granted loan / pays back

Orange Population

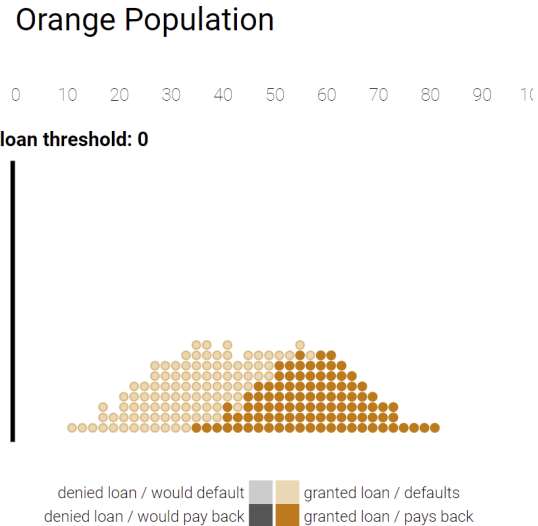
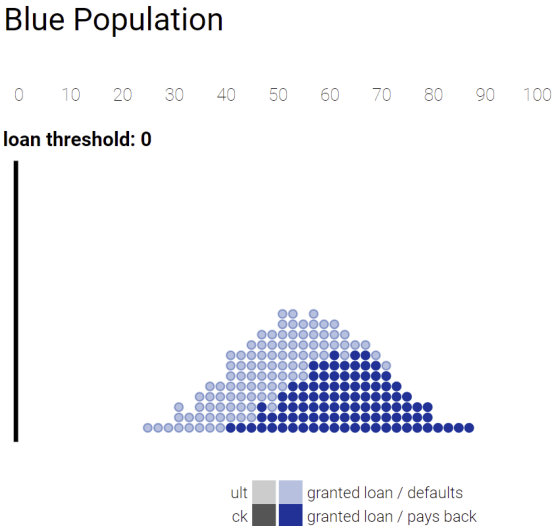
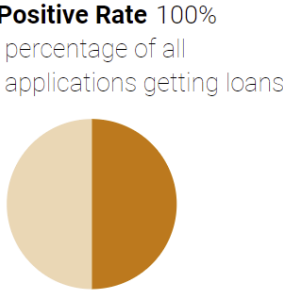
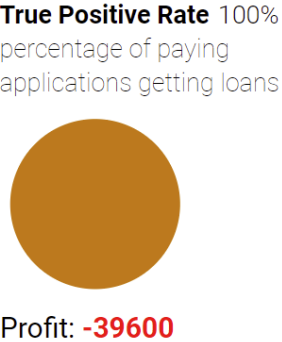
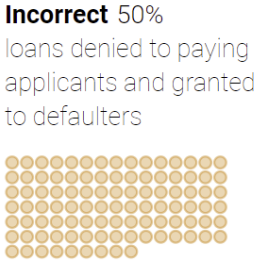
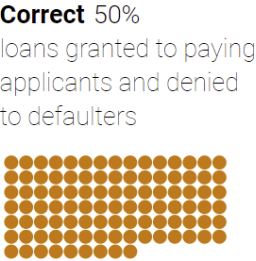
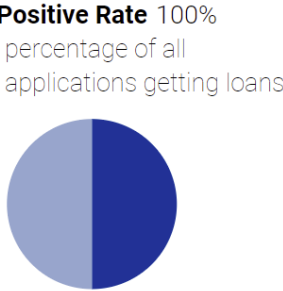
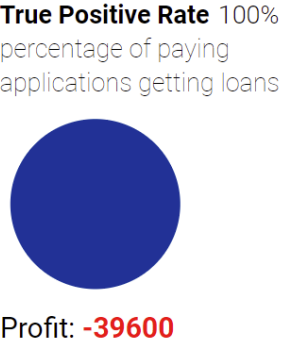
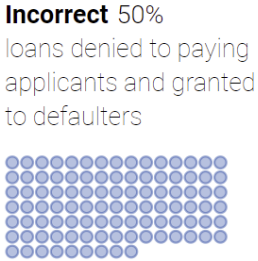
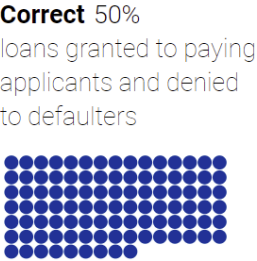
0 10 20 30 40 50 60 70 80 90 100

loan threshold: 0



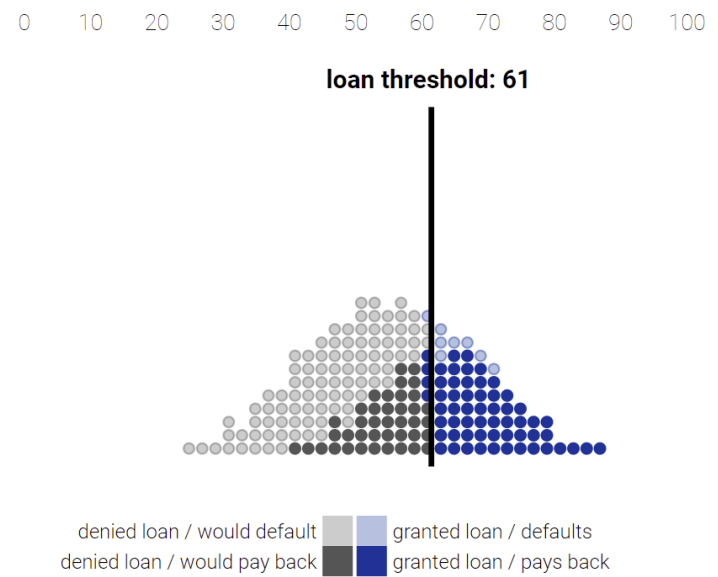
denied loan / would default light orange
denied loan / would pay back dark orange granted loan / defaults
granted loan / pays back

Total profit = -79200

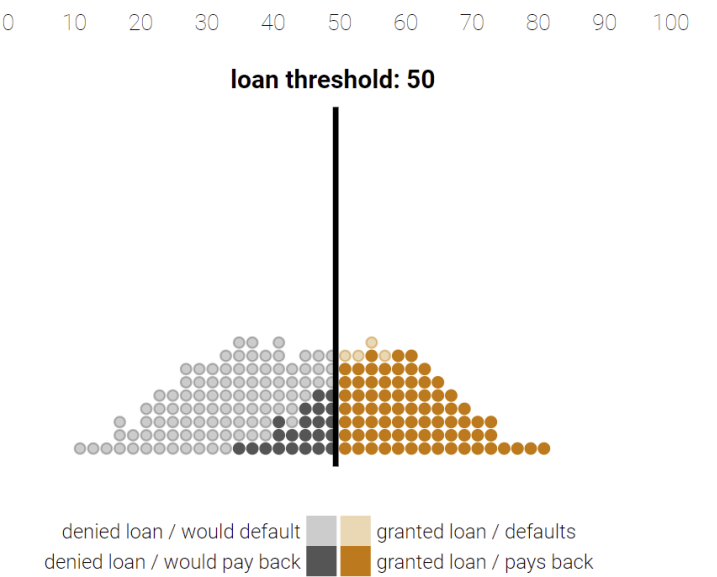


Maximize profit

Blue Population

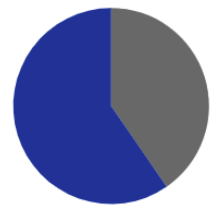


Orange Population



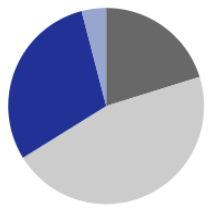
Total profit = 32400

True Positive Rate 60%
percentage of paying
applications getting loans

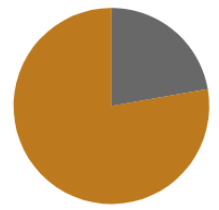


Profit: 12100

Positive Rate 34%
percentage of all
applications getting loans



True Positive Rate 78%
percentage of paying
applications getting loans



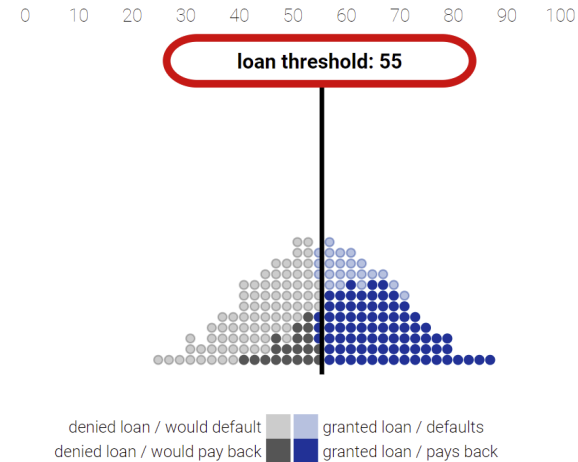
Profit: 20300

Positive Rate 41%
percentage of all
applications getting loans

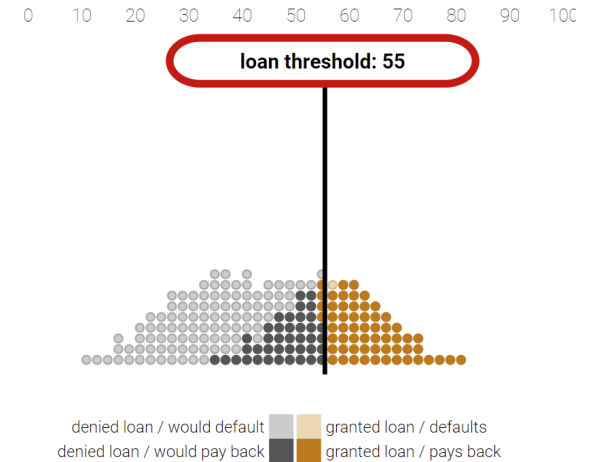


Ignore group

Blue Population

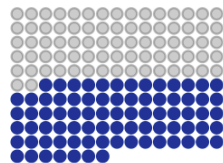


Orange Population



Calibrated from
lender POV

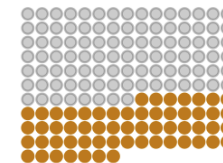
Correct 79%
loans granted to paying
applicants and denied
to defaulters



Incorrect 21%
loans denied to paying
applicants and granted
to defaulters



Correct 79%
loans granted to paying
applicants and denied
to defaulters

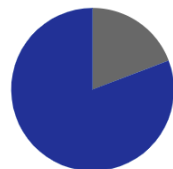


Incorrect 21%
loans denied to paying
applicants and granted
to defaulters



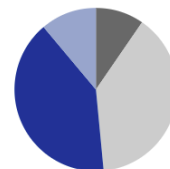
Unfair from
applicant POV

True Positive Rate 81%
percentage of paying
applications getting loans

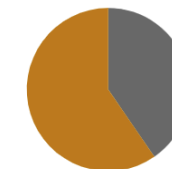


Profit: **8600**

Positive Rate 52%
percentage of all
applications getting loans

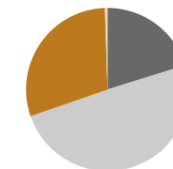


True Positive Rate 60%
percentage of paying
applications getting loans



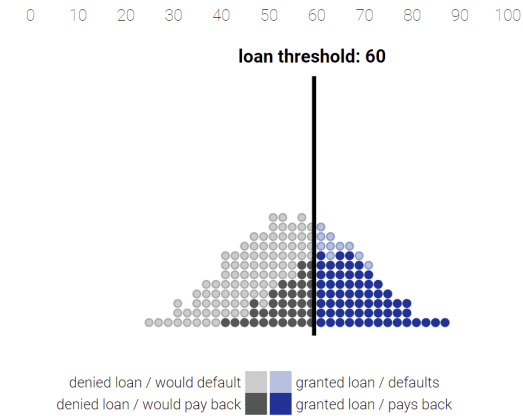
Profit: **17000**

Positive Rate 30%
percentage of all
applications getting loans

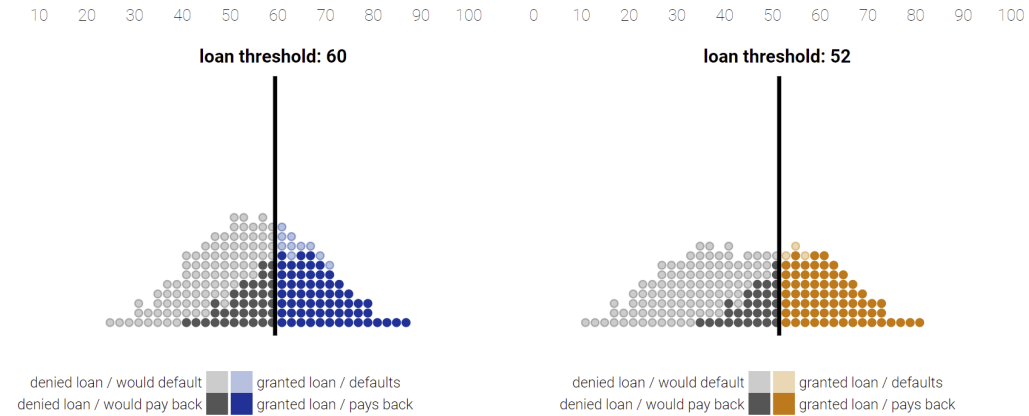


Demographic parity

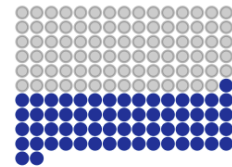
Blue Population



Orange Population



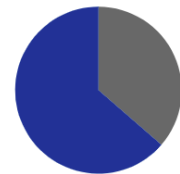
Correct 77%
loans granted to paying
applicants and denied
to defaulters



Incorrect 23%
loans denied to paying
applicants and granted
to defaulters

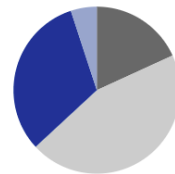


True Positive Rate 64%
percentage of paying
applications getting loans

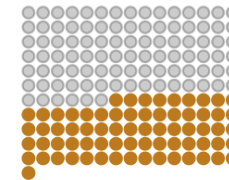


Profit: 11900

Positive Rate 37%
percentage of all
applications getting loans



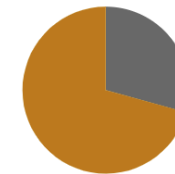
Correct 84%
loans granted to paying
applicants and denied
to defaulters



Incorrect 16%
loans denied to paying
applicants and granted
to defaulters

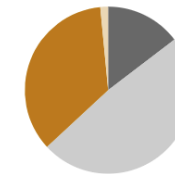


True Positive Rate 71%
percentage of paying
applications getting loans



Profit: 18900

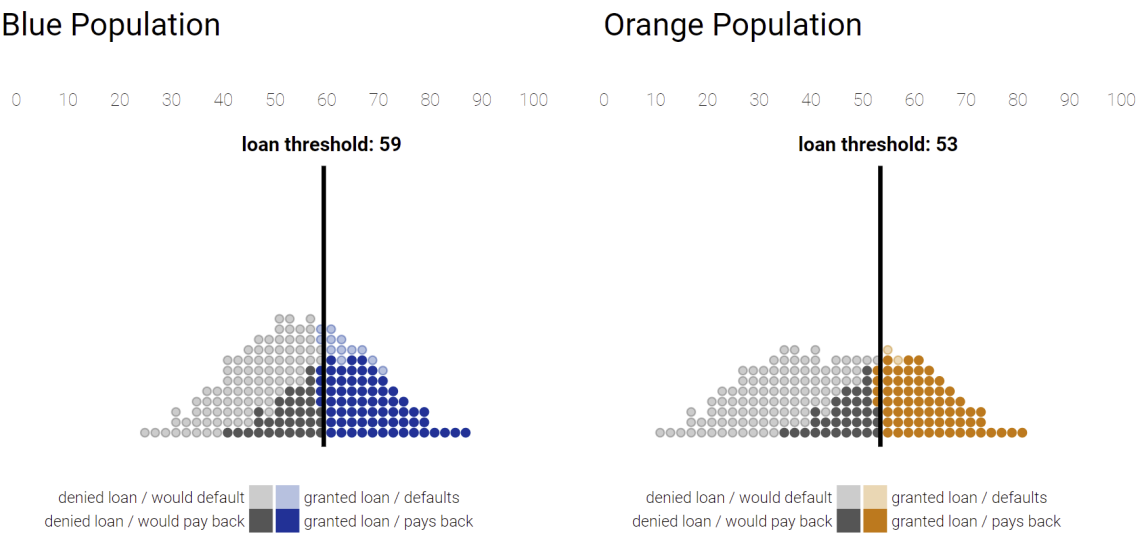
Positive Rate 37%
percentage of all
applications getting loans



Same total loans

Accuracy
advantage split
between lender
and applicant

Equal opportunity



denied loan / would default

denied loan / would pay back

granted loan / defaults

granted loan / pays back

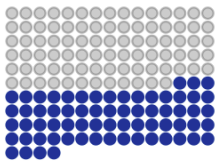
denied loan / would default

denied loan / would pay back

granted loan / defaults

granted loan / pays back

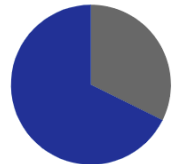
Correct 78%
loans granted to paying applicants and denied to defaulters



Incorrect 22%
loans denied to paying applicants and granted to defaulters



True Positive Rate 68%
percentage of paying applications getting loans

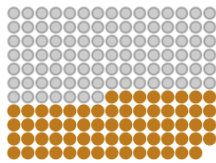


Profit: 11700

Positive Rate 40%
percentage of all applications getting loans



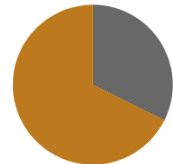
Correct 83%
loans granted to paying applicants and denied to defaulters



Incorrect 17%
loans denied to paying applicants and granted to defaulters



True Positive Rate 68%
percentage of paying applications getting loans



Profit: 18700

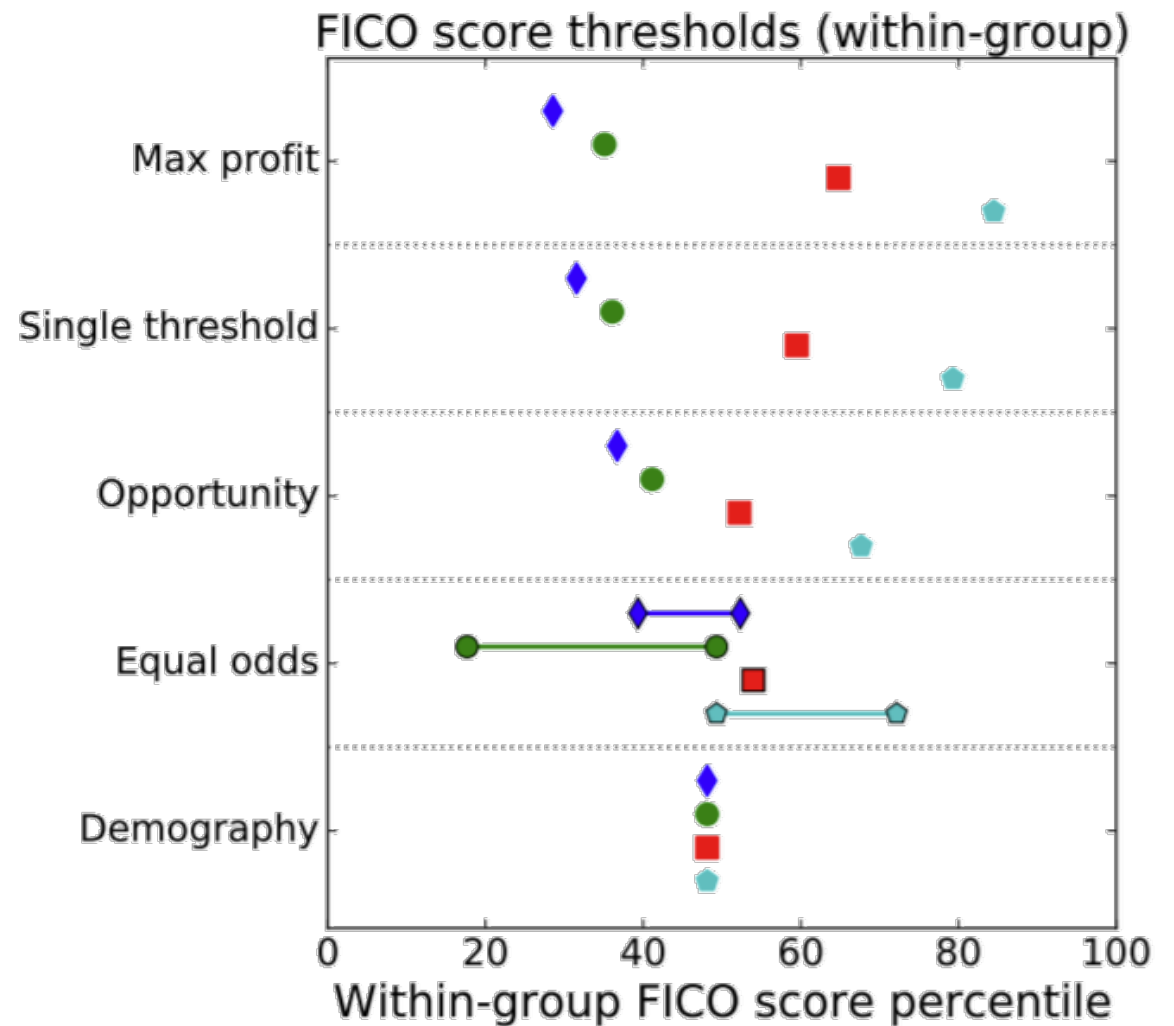
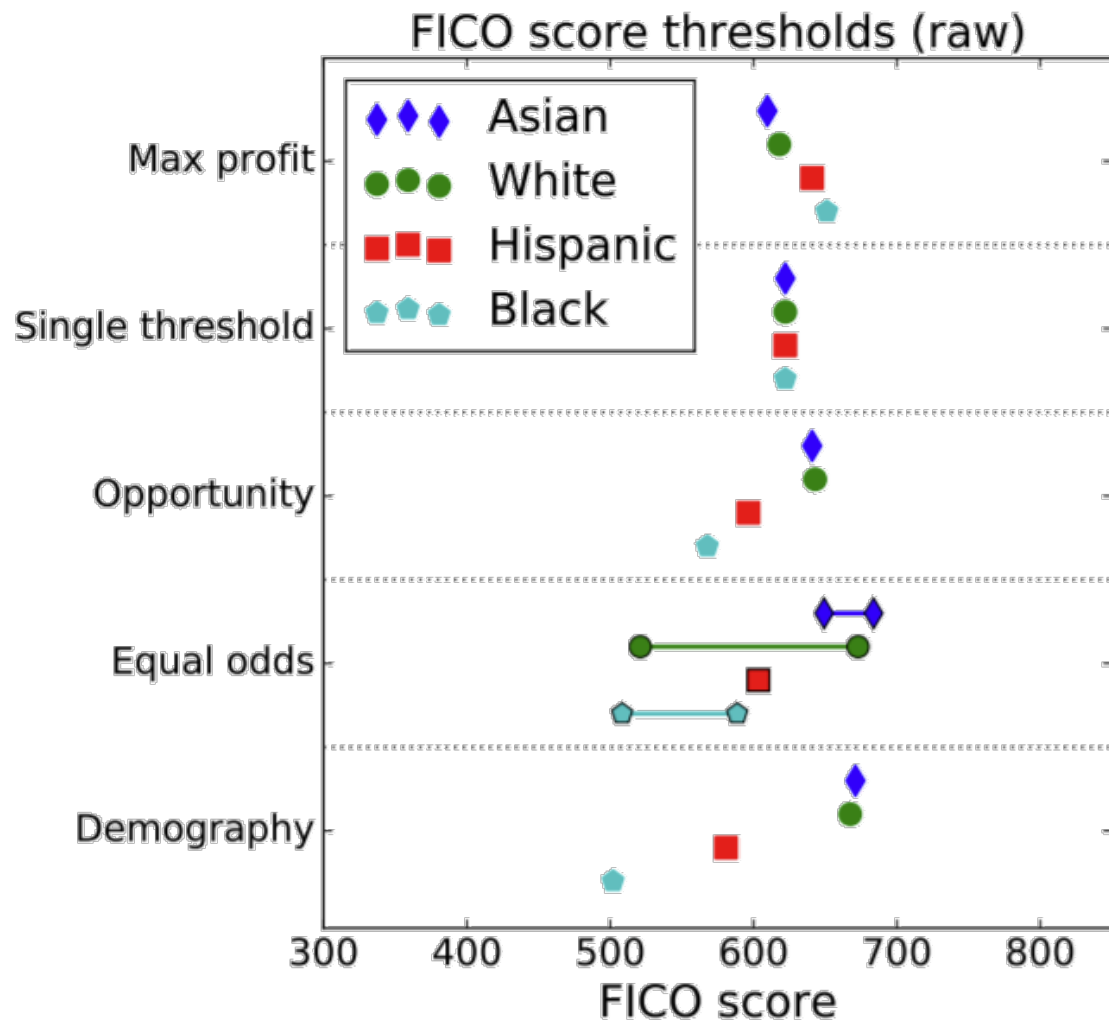
Positive Rate 35%
percentage of all applications getting loans



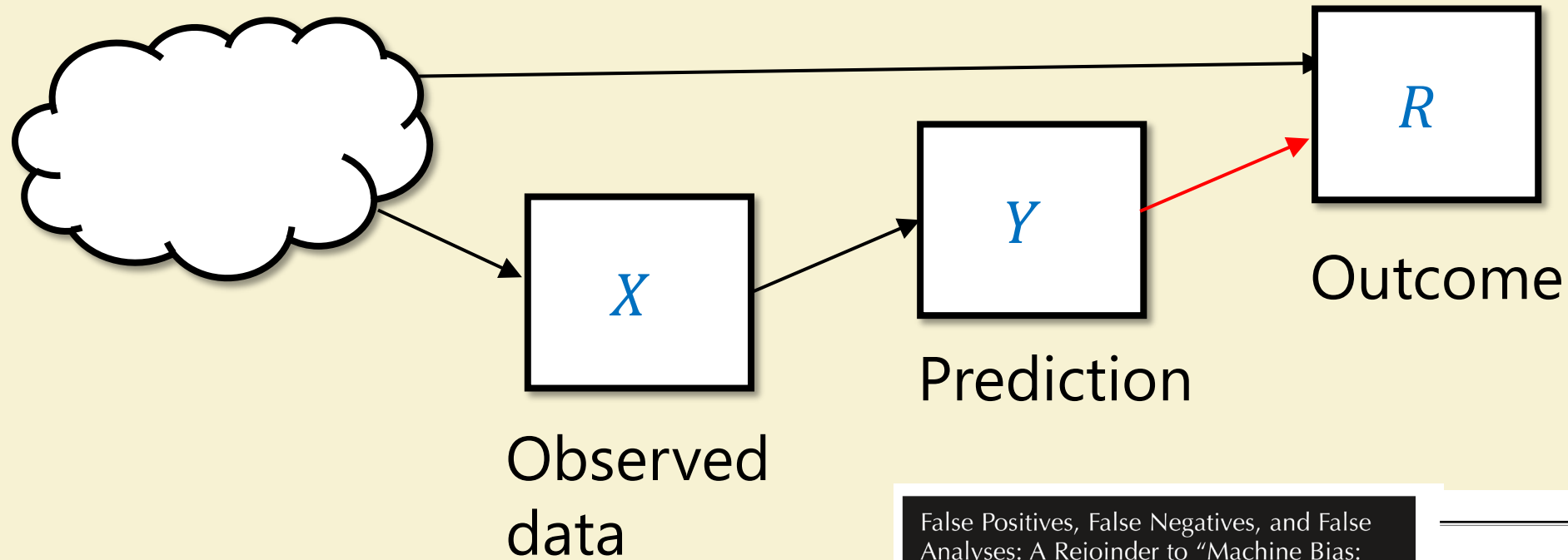
No demographic parity

Fair from applicant POV

Real world example: FICO scores



COMPAS Debate



False Positives, False Negatives, and False Analyses: A Rejoinder to "Machine Bias: There's Software Used Across the Country to Predict Future Criminals. And It's Biased Against Blacks."

Anthony W. Flo,
California State University, Bakersfield
Kristin Bech
Crime and Justice Institute at C
Christopher T. Lowenkamp
Administrative Office of the United States Cour
Probation and Pretrial Services Off

COMPAS Risk Scales:
Demonstrating
Accuracy Equity and Predictive Parity

PERFORMANCE
OF THE COMPAS RISK SCALES
IN BROWARD COUNTY

NORTHPOINTE INC.
RESEARCH DEPARTMENT

WILLIAM DIETERICH, PH.D.
CHRISTINA MENDOZA, M.S.
TIM BRENNAN, PH.D.

JULY 8, 2016

	WHITE	AFRICAN AMERICAN
Labeled Higher Risk, But Didn't Re-Offend	23.5%	44.9%
Labeled Lower Risk, Yet Did Re-Offend	47.7%	28.0%

Angwin, Larson, Mattu, Kirchner 2016

Data*

Did not recidivate

Recidivate

Black

Low Risk	High Risk
1000	800
550	1400

White

Low Risk	High Risk
1150	350
450	500

Defendant POV

$\Pr[HR | No\ rec.]$

$$\frac{800}{1800} \approx 44\%$$

>

$$\frac{350}{1450} \approx 24\%$$

Predictor POV

$\Pr[No\ Rec. | HR]$

$$\frac{800}{2200} \approx 36\%$$

<

$$\frac{350}{850} \approx 41\%$$

Fairness and causality

Berkeley graduate admissions, 1973

44% of male applicants admitted

35% of female applicants admitted

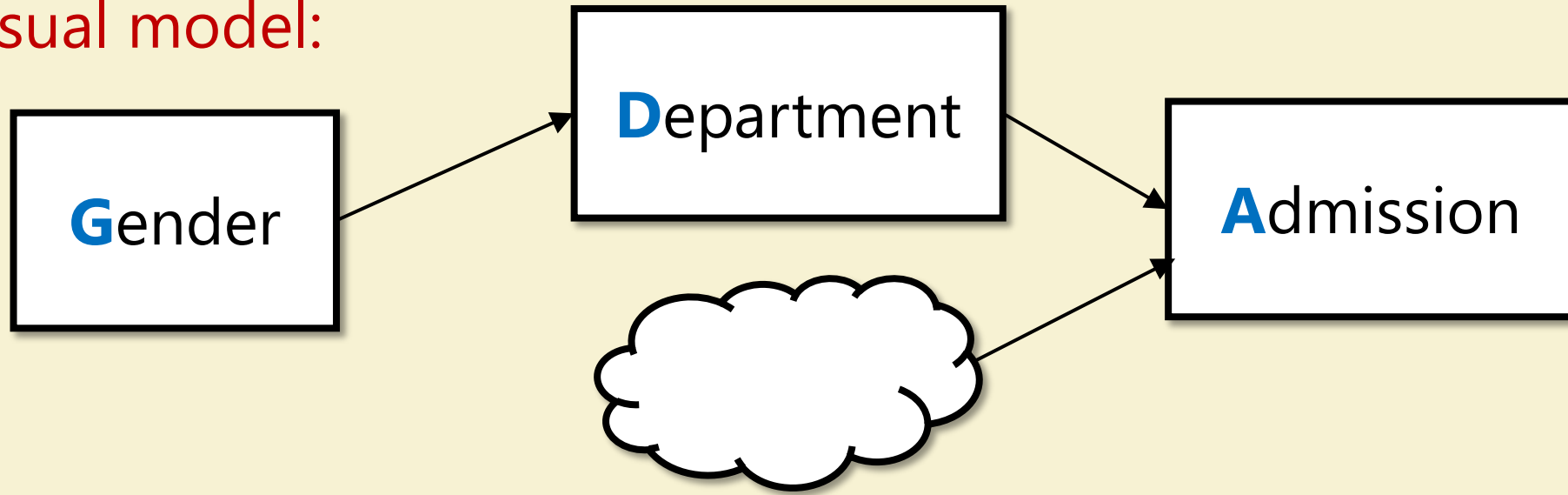
Department level:

Female acceptance rate *higher*

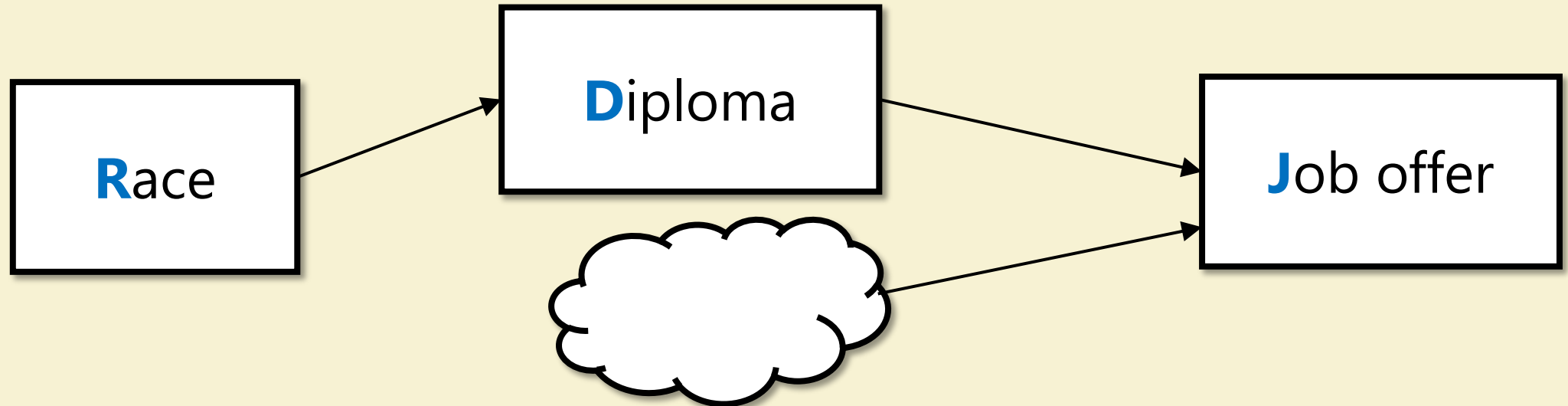
UC Berkeley admissions data from 1973.

Department	Men		Women	
	Applied	Admitted (%)	Applied	Admitted (%)
A	825	62	108	82
B	520	60	25	68
C	325	37	593	34
D	417	33	375	35
E	191	28	393	24
F	373	6	341	7

"Fair" casual model:



Content of boxes matter (e.g. Griggs v. Duke Power Co., 1971)

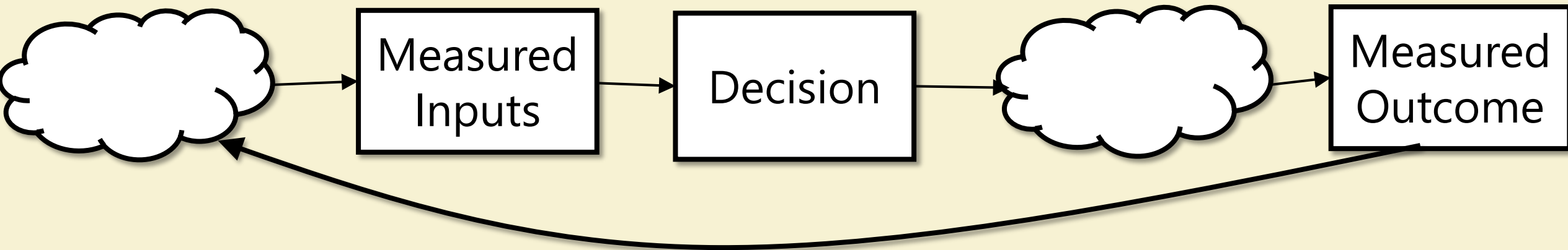


Bottom line

Can't come up with **universal observational** fairness criteria

Fairness is based on **assumptions** on:

- Representation of data
- Relation to **unmeasured** inputs and outcomes
- Causal relation of inputs, predictions, outcomes



Left: Construct spaces are idealized versions of features and decisions and may be unobservable.

Right: Observed spaces are the typical inputs (features) and outputs (decisions) of machine learning procedures.

